

**Math 121A Spring 2009**  
**Homework#8** Poles, Laurent series, Residue theorem.

1. Write the Laurent series of  $f$  around  $z_0$  and compute its radius of convergence for

(a)  $f(z) = \frac{1}{z(z-1)(z+1)}$  and  $z_0 = -1, 0, 1$ .

(b)  $f(z) = \frac{z+3}{z^2(z-1)^3(z+1)}$  and  $z_0 = -1, 0, 1$ .

(c)  $f(z) = \frac{e^z}{z^3}$ ,  $z_0 = 0$ .

(d)  $f(z) = \frac{\sin^2 z}{z^3}$ ,  $z_0 = 0$ .

2. Compute the residue  $\text{res}_{z_0}(f)$  for the cases in Problem 1 above.

3. Write the definition (given in class) of a regular point, essential singularity, pole, and order of a pole of a function  $f(z)$  at a point  $z_0$ . Solve Problems 9, 10, 11 in M. Boas book, page 682.

4. For the functions of Problem 1 compute  $\int_C f(z)dz$  where  $C$  is the circle of radius 10 in the plane.

• **Remarks**

- You are very much encouraged to work with other students. However, submit your work alone.
- I will be happy to help you with the homeworks. Please visit me if you want to work with me.

**Good luck!**