## CS/ECE/MATH 435: HOMEWORK 6, DUE MANUEL.

- 1. An RSA cryptosystem has public key N=35 and e=7. Messages are encrypted one letter at a time, converting letters to numbers by A=2, B=3, ..., Z=27, space = 28.
  - (a) Showing your working, encrypt the message: BE GOOD.
  - (b) Find the decryption exponent d and decrypt the message: 20 23 26 7 15 16
- (c) This choice of N and e has several weaknesses name at least two different ones.
- (d) Even if a good choice of N and e is made, the method of encrypting one letter at a time has weaknesses. Describe how we might find the plaintext if a very long eighertext is given.
- (e) Oscar intercepts the message 365, 0, 4845, 14930, 2608, 2608, 0 from Alice to Bob. How do you think they are converting letters to numbers? Decrypt the message.
- 2. (a) Suppose Alice sends the same message x (e.g. her credit card number), encrypted, to three companies, all of which use the easy choice of e=3 in their public key. Oscar intercepts these encrypted messages, i.e.  $x^3 \pmod{N_1}, x^3 \pmod{N_2}, x^3 \pmod{N_3}$ , where  $N_1, N_2, N_3$  are the moduli used in the companies' public keys. There is a method (the Chinese Remainder Theorem) by which he can deduce the value of  $x^3 \pmod{N_1N_2N_3}$ . Why can he now compute x exactly? This is why e=3 is a poor choice in practice.
  - (b) A popular choice for e is 65537. Why is this a good choice in practice?