(a) Show the general solution of the PDE  $u_{xy} = 0$  is

$$u(x,y) = F(x) + G(y)$$

for arbitrary functions F, G.

- (b) Using the change of variables  $\xi = x + t$ ,  $\eta = x t$ , show  $u_{tt} u_{xx} = 0$  if and only if  $u_{\xi\eta} = 0$ .
- (c) Use (a) and (b) to rederive d'Alembert's formula.