$2.5 \ \#9$

Let u be the solution of

$$\begin{cases} \Delta u = 0 & \text{in } \mathbb{R}^n_+ \\ u = g & \text{on } \partial \mathbb{R}^n_+ \end{cases}$$

given by Poisson's formula for the half-space. Assume g is bounded and g(x) = |x| for $x \in \partial \mathbb{R}^n_+$, $|x| \leq 1$. Show Du is not bounded near x = 0. Hint: Estimate $\frac{u(\lambda e_n) - u(0)}{\lambda}$.