

**HOMEWORK #3**

Calculate the fundamental group of the spaces below:

- (1) The complement in  $\mathbb{R}^3$  of a line and a circle. Note: There are two cases to consider, one where the line goes through the interior of the circle and the other where it doesn't. Are these two spaces homotopy equivalent?
- (2) The complement in  $\mathbb{R}^3$  of a line and a point not on the line.
- (3)  $\mathbb{R}^3$  minus two disjoint lines.
- (4)  $T^2 \setminus \{x, y\}$ , where  $x, y$  are two distinct points on the 2-torus  $T^2$ .
- (5) Klein bottle  $K$ . Are the torus and the Klein bottle homotopy equivalent?
- (6) real projective plane  $\mathbb{R}P^2$ .