HOMEWORK #2

Calculate the fundamental group of the spaces below:

(1) A 2-sphere with a diameter attached to it.
(2) A 2-sphere with the ecuatorial disc attached to it.
(3) The complement in $\mathbb{R}^3$ of a line and a circle. Note: There are two cases to consider, one where the line goes through the interior of the circle and the other where it doesn't. Are these two spaces homotopy equivalent?
(4) The complement in $\mathbb{R}^3$ of a line and a point not on the line.
(5) $\mathbb{R}^3 \setminus \{x - \text{axis } \textit{and } y - \text{axis}\}$.
(6) $\mathbb{R}^3$ minus two disjoint lines.
(7) $T^2 \setminus \{x, y\}$, where x, y are two distinct points on the 2-torus.
(8) Möbius band. Are the cylinder and the Möbius band homeomorphic?