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Dear Professor Miller

I read your letter about the problem published in American Mathematical Monthly p 280, and I'm delighted by your „almost" decomposition theorem. I follow your arguments and I hope that you can extend them easy from the case when $(R,+)$ is rempleced by a group $(G,*)$ which is not finitely generated. For finite groups $(G,*)$ is possible that $f: G \to G$ cannot be written

$$f = g_1 * \dots * g_n(x) \quad , g_k \text{ bijections } g_k : G \to G$$

where $(g * h)(x) = g(x) * h(x)$.
By example $G = \mathbb{Z}_n$, $n \geq 3$. Also from your results it follows easy that:

$$\left[\begin{array}{l} \text{For every } f: R \to R \text{ there exists bijective functions} \\ g_1, g_2, g_3 : R \to R \text{ such } \quad f = g_1 + g_2 + g_3 \end{array} \right]$$

I'm interested especially in the case when the algebraic topologic aspects are primordial. By example

<u>Problem</u> $f: \mathcal{T} \to \mathcal{T}$ continue

There exist n homeomorphisms $g_1, \dots, g_n : \mathcal{T} \to \mathcal{T}$

$$f = g_1 + \dots + g_n$$

$\mathcal{T}$ has a compatible structure of topologic group.

I thank you for the interes in this field, and I'll be glad to know if you want to colaborate.

Sincerely yours

Louis Funar, Univ Craiova, Craiova, Romania