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A. Miller Math 331

03/19/2012

Homework for 03-19

48 A

49 A

50 A

03-19-(48) by (11/11/12)

$P(|X - \mu| \geq \epsilon) \leq \frac{\sigma^2}{\epsilon^2} \Rightarrow P(|X - \mu| < \epsilon) \geq 1 - \frac{\sigma^2}{\epsilon^2}$
given that X is a series of independent trials

$$P(|X - np| < \epsilon) \geq \frac{1 - np(1-p)}{\epsilon^2}$$

Now let $\epsilon = .01n = \frac{n}{100}$

$$P\left(|X - \frac{n}{2}| < \frac{n}{100}\right) \geq 1 - \frac{n \cdot 2 \cdot \frac{1}{10000}}{n^2} = 1 - \frac{20,000}{n}$$

For this prob. to be 99% $1 - \frac{20,000}{n} \text{ must} = .99$

so,

$$\frac{-20,000}{n} = .99 - 1$$

$$-20,000 = -.01n$$

$$n = \frac{20,000}{.01} = \boxed{2,000,000}$$



03-19-(49)

$$X \geq 0 \quad \mu = E(X) \quad P(X < 3) < \frac{1}{3}$$

$$P(X \geq \alpha) \leq \frac{\mu}{\alpha} \quad \text{Markov's Inequality}$$

∴

$$\mu \geq \alpha P(X \geq \alpha) \text{ so } \mu \geq 3P(X \geq 3)$$

$$\text{as } P(X < 3) < \frac{1}{3} \quad P(X \geq 3) \geq \frac{2}{3}$$

$$\mu \geq 3 \cdot P(X \geq 3) \geq \boxed{\frac{12}{3}}$$

cont. on next side.

03-19-50

$$a.) P(-2\sigma < X - \mu < 2\sigma) \\ = P(|X - \mu| < 2\sigma)$$

by Chebyshev's inequality

$$P(|X - \mu| < \epsilon) \geq 1 - \frac{\sigma^2}{\epsilon^2}$$

$$\therefore P(|X - \mu| < 2\sigma) \geq 1 - \frac{\sigma^2}{4\sigma^2} = \frac{3}{4} \geq .75 \checkmark$$

b.) Let ϵ be 3σ

so

$$P(|X - \mu| < 3\sigma) \geq 1 - \frac{\sigma^2}{9\sigma^2} = \frac{8}{9} = .\bar{8} \geq .88 \checkmark$$

$$\therefore P(|X - \mu| < 3\sigma) \geq .88$$