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Mar 16 (47) A basketball player has $\frac{1}{2}$ chance of making 1pt free throw
A $\frac{1}{3}$ chance of 2pt shot, $\frac{1}{5}$ chance of 3pt. In a game
he makes 10 1pt attempts, 21 2pt attempts, 5 3pt attempts

X = total number of pts he scores. Find $E(X)$, $\text{var}(X)$, $\text{sd}(X)$

A = number of 1 point shot successes

B = " " 2 point "

C = " " 3 point "

$$X = A + 2B + 3C$$

$$E(X) = E(A) + 2E(B) + 3E(C) = 10\left(\frac{1}{2}\right) + 2(21)\left(\frac{1}{3}\right) + 3(5)\left(\frac{1}{5}\right) = 5 + 14 + 3 = 22$$

$$\text{var}(A) = 10\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = 2.5$$

$$\text{var}(B) = 21\left(\frac{1}{3}\right)\left(\frac{2}{3}\right) = \frac{42}{9} = \frac{14}{3}$$

$$\text{var}(2B) = 4\text{var}(B) = \frac{56}{3}$$

$$\text{var}(C) = 5\left(\frac{1}{5}\right)\left(\frac{4}{5}\right) = \frac{4}{5}$$

$$\text{var}(3C) = 9\text{var}(C) = \frac{36}{5}$$

$$\text{var}(X) = 2.5 + \frac{56}{3} + \frac{36}{5} = 28.3\bar{6} = \frac{851}{30}$$

$$\text{sd}(X) = \sqrt{\frac{851}{30}}$$

