

Four proofs of Pythagorus's Theorem

1. Popular Ureka proof - Consider the top two squares and remove the four triangles.

2. Use the figure on top left and some algebra:

$$(a+b)^2 = c^2 + 4(\frac{ab}{2})$$

3, Use the figure on bottom right and some algebra. Middle square has side b - a so

$$c^{2} = (b-a)^{2} + 4(\frac{ab}{2})$$

4. This one is apparently in Euclid. Use the figure on the bottom left. Draw a perpendicular from the right angle to the hypotenuse splitting c into x plus y. The two inner triangles are similar to the big triangle. Using similar triangles write a/c = x/a and b/c = y/b. Solving algebraically to get $c = x + y = a^2/c + b^2/c$.