

No books, no notes, no electronic devices of any kind.  
Show all your work, simplify your answer, and circle it.

Name\_\_\_\_\_

Circle your TA's name and the time of your section.

Clement, Nathan	M	11:00	1:20
Jefferis, Leland	M	1:20	2:25
Makuluni, Edson	T	8:50	9:55
Nan, Ting-Ting	T	11:00	12:05
Wang, Kejia	M	8:50	9:55
Yao, Chengjian	T	1:20	2:25
You, Qian	T	11:00	12:05
Zhao, Yongqiang	M	8:50	11:00

Hand in to your TA.

Page	Points	Score
1	10	
2	10	
3	10	
4	10	
5	10	
6	10	
7	10	
8	10	
9	10	
10	10	
Total	100	

1. (10 pts) For each of the following circle your answer.

(a) Determine the domain of the function  $g(x) = \frac{x}{x^2-1}$ .

(b) Determine the domain of the function  $h(x) = (x^2 - 1)(x - 3)$ .

2. (10 pts) Find the points of intersection (if any) of the curves:

$$y = x^2 \text{ and } y = x + 2$$

Draw the graphs of these curves and label the points of intersection.

3. (10 pts) Find the equation for the line thru the points  $(1, -2)$  and  $(3, 4)$ . Draw the graph of this line and label these two points and label the  $x$  and  $y$  intercepts.

4. (10 pts) For what value of  $A$  (if any) is the following function  $f$  continuous for every  $x$ ? Circle your answer.

$$f(x) = \begin{cases} \frac{3}{x} & \text{if } x \geq 1 \\ x^2 + Ax - 2 & \text{if } x < 1 \end{cases}$$

5. (10 pts) Find the derivative of  $f$  using the definition of derivative. Begin by stating the definition of  $f'(x)$ .

$$f(x) = x^2 - 3x$$

Do **not** use differentiation rules. This problem is from Section 2.1. In all other problems you may use the differentiation rules to compute derivatives.

6. (10 pts) Find the derivative  $\frac{dz}{dt}$ , simplify it, and circle your answer.

$$z = \frac{3}{t^2} - \sqrt[5]{3t^2 - 1}$$

7. (10 pts) Find the second derivative of  $y$  with respect to  $x$ . Use the correct notation for the second derivative. Simplify your answer and circle it.

$$y = x^5 + 3x^3 - x^2 - 2x + 12$$



8. (10 pts) Suppose  $y$  is implicitly defined as a function of  $x$  by the equation:

$$y^2 + 2xy + x^3 = 13$$

- (a) Find  $\frac{dy}{dx}$  when  $x = 2$  and  $y = 1$ .
- (b) Use it to estimate the change in  $y$  when  $x$  is changed from 2 to  $2\frac{1}{7}$ .

9. (10 pts) A tumor is modeled as being roughly spherical with radius  $r$ . If the radius of tumor is currently  $r = 5$  milometers and growing at the rate of  $\frac{1}{2}$  milometer per month what is the corresponding rate of change of its volume  $V = \frac{4}{3}\pi r^3$ ?

10. (10 pts) For each of these circle the best answer.

1.  $\lim_{x \rightarrow 2^+} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

2.  $\lim_{x \rightarrow \infty} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

3.  $\lim_{x \rightarrow -\infty} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

4.  $\lim_{x \rightarrow -\infty} x^2 + x + 1$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

5.  $\lim_{x \rightarrow 0^+} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

6.  $\lim_{x \rightarrow 0^-} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

7.  $\lim_{x \rightarrow \infty} \frac{1}{1-x^2}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

8.  $\lim_{x \rightarrow 0} \frac{1}{x}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

9.  $\lim_{x \rightarrow 0} \frac{1}{x^2}$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

10.  $\lim_{x \rightarrow 1^-} x^2 + 1$   
0 1 2  $\infty$   $-\infty$  doesn't-exist none-of-these

## Answers

1. (a) all real numbers  $x$  except  $x = 1$  and  $x = -1$ . (b) all real numbers

2.  $(-1, 1)$  and  $(2, 4)$

3.  $y = 3x - 5$

4.  $A = 4$

5. Define

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

then

$$\begin{aligned} f(x+h) - f(x) &= ((x+h)^2 - 3(x+h)) - (x^2 - 3x) \\ &= x^2 + 2hx + h^2 - 3x - 3h - x^2 + 3x \\ &= 2hx + h^2 - 3h \end{aligned}$$

so

$$\frac{((x+h)^2 - 3(x+h)) - (x^2 - 3x)}{h} = \frac{2hx + h^2 - 3h}{h} = 2x + h - 3$$

so

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} (2x + h - 3) = 2x - 3$$

6.

$$\frac{dz}{dt} = -6t^{-3} - \frac{6}{5}t(3t^2 - 1)^{-\frac{4}{5}}$$

7.

$$\frac{d^2y}{dx^2} = 20x^3 + 18x - 2$$

8. (a)  $-\frac{7}{3}$  (b)  $-\frac{1}{3}$

9.  $50\pi$

10. none-of-these  $0$   $0$   $\infty$   $\infty$   $-\infty$   $-\infty$  doesn't-exist  $\infty$   $2$