Show all work. Simplify your answer. Circle your answer.

No books, no calculators, no cell phones, no pagers, no electronic devices of any kind.

Name

Circle your Discussion Section:

343	T	12:0512:55	1412	STERLING
344	R	12:0512:55	1327	STERLING
345	T	13:2014:10	1327	STERLING
346	R	13:2014:10	1327	STERLING

Problem	Points	Score
1	10	
2	10	
3	10	
4	10	
5	10	
6	10	
7	10	
Total	70	

Solutions will be posted shortly after the exam: www.math.wisc.edu/ \sim miller/m210

1. (10 pts) State the three Axioms for a Probability Measure:

A probability measure assigns to each event E of a sample space S a number denoted by Pr[E] and called the probability of E. This assignment must satisfy the three axioms:

i.

ii.

iii.

2. (10 pts) There are 9 mice in a cage: 3 white males, 4 gray females, and 2 gray males. Two mice are selected simultaneously and at random. Find the probability that at least one mouse is a male, given that at least one is gray.

3. (10 pts) There are 5 quarters, 1 dime, and 3 nickels in a drawer. An experiment consists of selecting a coin at random, noting its value, and setting it aside. If it is a dime, the experiment ends. If it is not a dime, then another coin is selected at random, and its value noted. Find the probability that at least one nickel is selected.

4. (10 pts) Students are being tested for Virus X and it is estimated that one percent of the students are infected. If a student is infected, the test is positive 80% of the time. If a student is not infected, the test is negative 90% of the time. If the test is applied to a student whose infection status is unknown, and if the test is negative, find the probability that the student is actually infected with Virus X.

5. (10 pts) A high school basketball player makes one-third of his three-point shots. If we assume that his shots are Bernoulli trails, how many must he shoot to have a probability of at least 3/4 of making at least one of them?

6. (10 pts) A carnival game consists of selecting 3 balls simultaneously and at random from a box containing 3 red and 5 green balls. Each red ball pays 50 cents each green ball pays 10 cents. It costs 1 dollar to play. A random variable X is the net payoff, i.e., prize money minus cost. Find the probability density function of X.

- 7. (10 pts) A coin is weighted so that the probability of **Heads** is 2/5. The coin is flipped ten times. Let X be the random variable which counts the number of **Tails** which come up. Find the
 - (a) expectation of X, $\mu = E(X)$

 $\mu =$

(b) the variance of X, $\nu = Var(X)$,

 $\nu =$

(c) and the standard deviation of X, $\sigma = SD(X)$.

 $\sigma =$

Answers

- 1. see page 88.
- 2.9/11
- 3. 13/24. This assumes that at most two selections were made which was what was intended. Some students interpreted the problem to mean that the experiment continues until a dime is selected. We may as well assume that the selection process stops whenever a nickel or dime is selected. Since any of the four stopping coins is equally likely to be the stop coin, the probability that the stop coin is a nickel is 3/4. This probability is the same whether there is 0 quarters or 100 quarters.
 - 4.2/893
 - 5. n = 4 this is the least n such that $(2/3)^n \le 1/4$.

6.

7.
$$\mu = 6, \nu = 12/5, \sigma = \sqrt{\nu}$$