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Journal Title: Linear & multilinear algebra.

Volume: 36 Issue: 2 Month/Year: 1993 Pages: 147-149

Article Author:

Article Title: Neumann, Michael; Corrections and additions to; "Principal components of minus \$M\$-matrices [Linear and Multilinear

OCLC Number: 2245998

Imprint: Philadelphia, etc. Gordon and Breach.

ILL Number: 26863251

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Linear and Multilinear Algebra, 1993, Vol. 36, pp. 147–149 Reprints available directly from the publisher Photocopying permitted by license only © 1993 Gordon and Breach Science Publishers S.A. Printed in Malaysia

Corrections and Additions to: "Principal Components of Minus *M*-Matrices"

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(Received March 11, 1993)

Professor Bit-Shun Tam has pointed to us that the statement of Lemma 2 and the proof of Lemma 1 in our paper which appeared in Vol. 32: 131–148, 1992, need correction and augmentation, respectively. We begin with the correction:

LEMMA 2 Let A be a minus M-matrix as in (2.1) and let i and j be vertices in $\mathcal{R}(A)$. Then $Z^{(d(i,j)-1)}[\{i,j\}] > 0$.

Proof First, by the Rothblum index theorem we have that $d(i,j) = \nu(A\{i,j\})$. Thus the result is a consequence of Lemma 1(i) and of the resolvent expansion of $A\{i,j\}$ which, in a sufficiently small punctured neighborhood of 0, satisfies that $(\epsilon I - A\{i,j\})^{-1} \ge 0, \forall \epsilon > 0$.

Next, we wish to clarify the proof of the latter part of Lemma 1(i) in which we claim that $Z^{(k)}[\langle i,j\rangle] = (A\{i,j\})^k Z_{A\{i,j\}}$. First it is a simple consequence of the first part of the claim that if q is any polynomial such that q(A) = 0, then $q(A\{i,j\}) = 0$. Whence, for every complex z such that $(zI - A)^{-1}$ exists, $(zI - A)^{-1}[\{i,j\}] = (zI - A\{i,j\})^{-1}$. We now express the resolvents of A and of $A\{i,j\}$ in terms of the principal components corresponding to their eigenvalues λ and we compare coefficients of $(z - \lambda)^{-s}$. It follows that $Z^{(k)}[\langle i,j\rangle] = (A\{i,j\})^k Z_{A\{i,j\}}$.

The proof we give in the paper for Corollary 1 establishes the weaker result below (and we do not know if Corollary 1 as stated originally is correct).

COROLLARY 1 Suppose A is a minus M-matrix given in form (2.1). If, for sufficiently small $\epsilon > 0$, a basis can be extracted for the columns of J given in (3.7) which satisfies (3.9), where $c_{k,j} \geq 0$, k, j = 1, ..., m, then (3.10) holds.

In fact, Corollary 1 as stated here can also be deduced from the more general result proved in [6, Cor. (3.17)].

We have not found a counter-example to Corollary 1 as stated originally. However, in what follows we give here an example which shows that an arbitrary choice of columns of J may yield a strongly combinatorial basis for the Perron space of A which however is not a semi-preferred basis:

F r i

Let

$$A = \begin{pmatrix} -1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & -1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{pmatrix}.$$

Then, with $\epsilon = 1/2$,

$$8J = \begin{pmatrix} 8 & 8 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 8 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 8 & 8 & 0 & 0 & 0 & 0 \\ 0 & 0 & 8 & 8 & 0 & 0 & 0 & 0 \\ 28 & 36 & 0 & 0 & 16 & 0 & 0 & 0 \\ 36 & 28 & 28 & 36 & 0 & 16 & 0 & 0 \\ 142 & 142 & 63 & 79 & 36 & 36 & 8 & 8 \\ 114 & 114 & 51 & 63 & 28 & 28 & 8 & 8 \end{pmatrix}.$$

Let B be the matrix obtained by choosing columns 1, 3, 5, 6, and 7 of J. Then the columns of B form a strongly combinatorial basis (in the sense of the paper) for the Perron space of A. However the matrix C which satisfies AB = BC (and which therefore contains the coefficients $c_{k,j}$ of (3.9)) is given by:

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1/2 & 0 & 0 & 0 & 0 \\ 1/2 & 1/2 & 0 & 0 & 0 \\ 0 & -1/4 & 1 & 1 & 0 \end{pmatrix}.$$

Since C has a negative entry, the basis given by B is not semi-preferred. Whereas, on choosing columns 1, 4, 5, 6, and 7 the matrix C so obtained is

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1/2 & 0 & 0 & 0 & 0 \\ 1/2 & 1/2 & 0 & 0 & 0 \\ 0 & 1/4 & 1 & 1 & 0 \end{pmatrix}.$$

Thus the columns of B are a semi-preferred basis for the Perron space of A.

We have a further relevant comment. The matrix J depends on a choice of ϵ . However, for any fixed choice of columns of J which form a basis B for the Perron space of A, it can be shown that the induced matrix C satisfying AB = BC is independent of ϵ .

We are very grateful to Professor Tam for spotting the necessity for the above corrections.